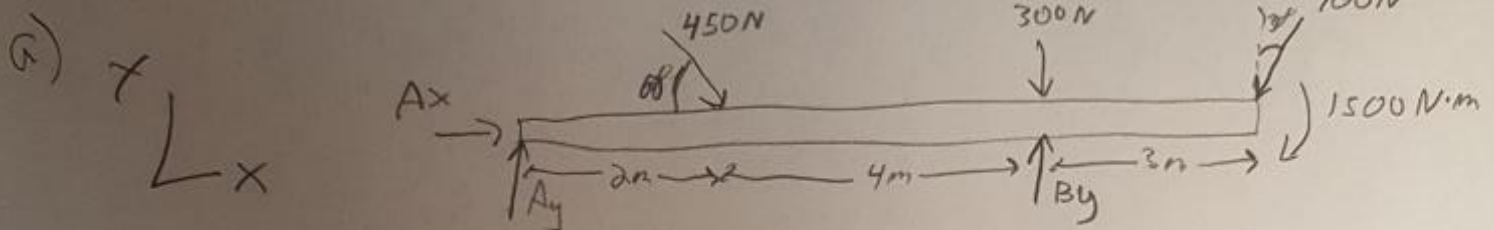
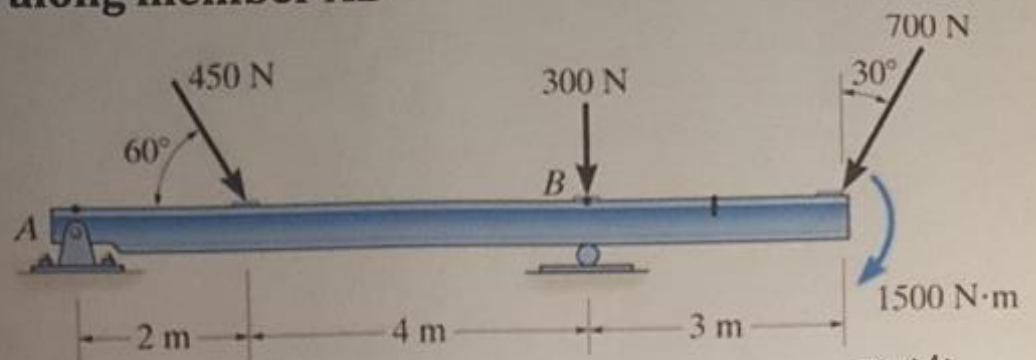


1a. Determine the Reactions at A and B

b. Replace the force moment system with an equivalent force and specify its location along member AB



$$\sum F_x = 0 = A_x + 450 \cos 60^\circ - 700 \sin 30^\circ$$

$$A_x = 125 \text{ N}$$

$$\sum F_y = 0 = A_y - 450 \sin 60^\circ - 300 - 700 \cos 30^\circ + B_y$$

$$\sum M_A = 0: \frac{450 \sin 60^\circ (2) + 300(6) + 700 \cos 30^\circ (9) + 1500}{6} = B_y$$

$$B_y = 1589.23 \text{ N}$$

$$A_y = -293.3 \text{ N}$$

negative about A

b)

$$M_{RA} = -9535.4 \text{ N}\cdot\text{m}$$

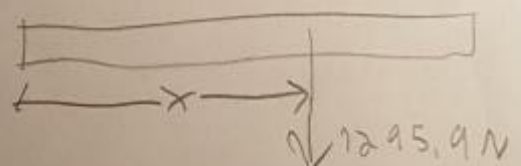
$$F_y = -1295.93 \text{ N}$$

$$F_x = 450 \cos 60^\circ - 700 \sin 30^\circ = -125 \text{ N}$$

$$M_{RA} = x F_y$$

$$-9535.4 = x (-1295.93)$$

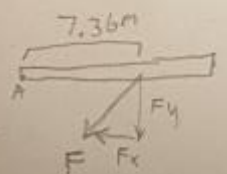
$$x = 7.36 \text{ m}$$



$$F = \sqrt{F_x^2 + F_y^2}$$

$$= \sqrt{(-125)^2 + (-1295.9)^2}$$

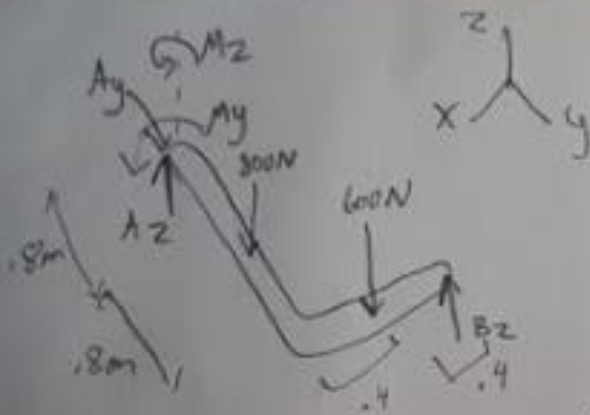
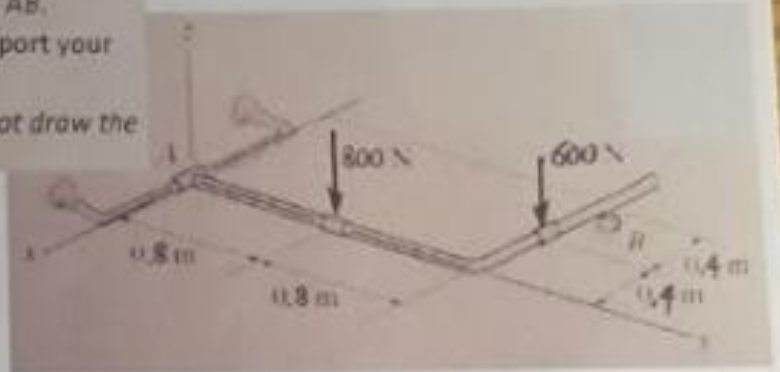
$$= 1302 \text{ N}$$



2. The weightless pipe assembly is supported in the horizontal plane by a smooth collar at A and rests on a smooth surface support at B. Two vertical forces are applied as shown.

- (a) Draw a free-body diagram of the pipe assembly AB.
 (b) Determine the support reactions at A and B. Report your answers in Cartesian vector form.

You will receive no credit for part (b) if you do not draw the free-body diagram.



$$\sum M_x = 0 = -800(0.8) - 600(1.6) + 1.6 B_z$$

$$B_z = 1000 \text{ N}$$

$$\sum F_x = 0$$

$$\sum F_y = 0 = A_y$$

$$\sum F_z = 0 = -800 - 600 = A_z + B_z$$

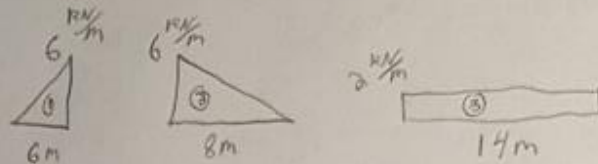
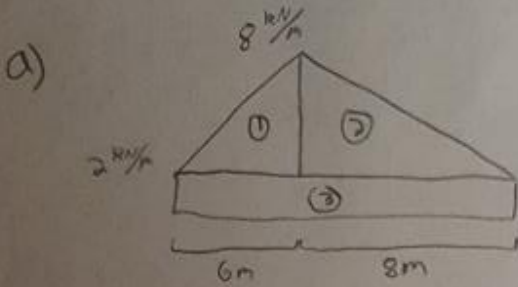
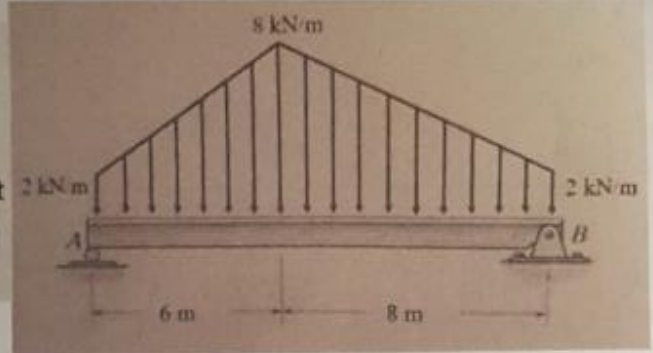
$$A_z = 400 \text{ N}$$

$$\sum M_y = M_y + 0.8 B_z - 600(0.4) = 0$$

$$M_y = -560 \text{ N}\cdot\text{m}$$

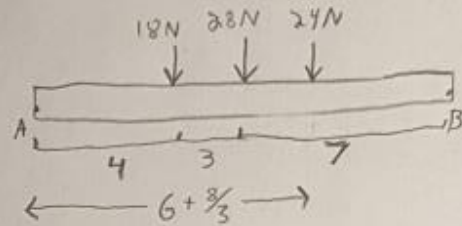
$$\sum M_z = 0 = M_z$$

3. The distributed load acts on the beam AB as shown.
- Determine the force-couple system at point A that is equivalent to the original distributed load.
 - Replace the original distributed load with an equivalent resultant force, and specify its location measured from point A.



$$\begin{aligned}
 F_R &= F_1 + F_2 + F_3 \\
 &= \frac{1}{2}(6)(6) + \frac{1}{2}(8)(6) + 2(14) \\
 &= 18 + 24 + 28 \\
 &= 70 \text{ kN}
 \end{aligned}$$

$$\vec{F}_R = -70 \text{ kN } \hat{R}$$

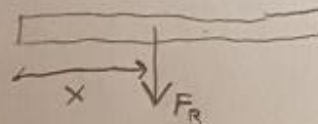


$$\begin{aligned}
 \Rightarrow M_{RA} &= -F_1 d_1 - F_2 d_2 - F_3 d_3 \\
 &= -18(4) - 28(7) - 24\left(6 + \frac{8}{3}\right) \\
 &= -476 \text{ kN}\cdot\text{m}
 \end{aligned}$$

b)

$$M_{RA} = x F_R$$

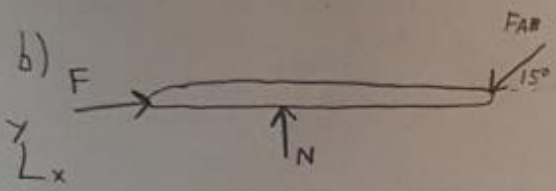
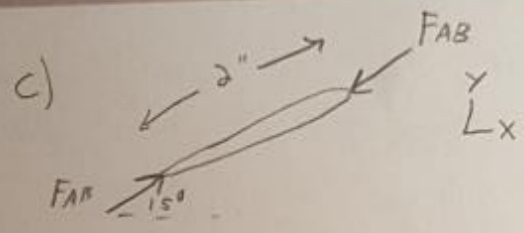
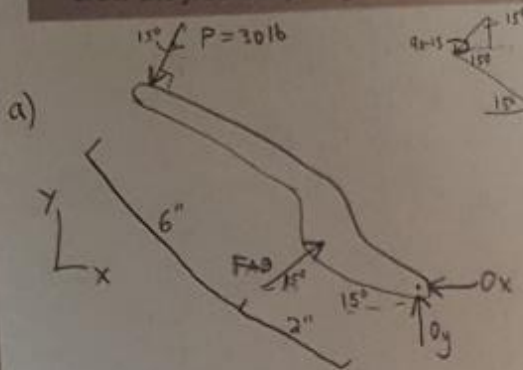
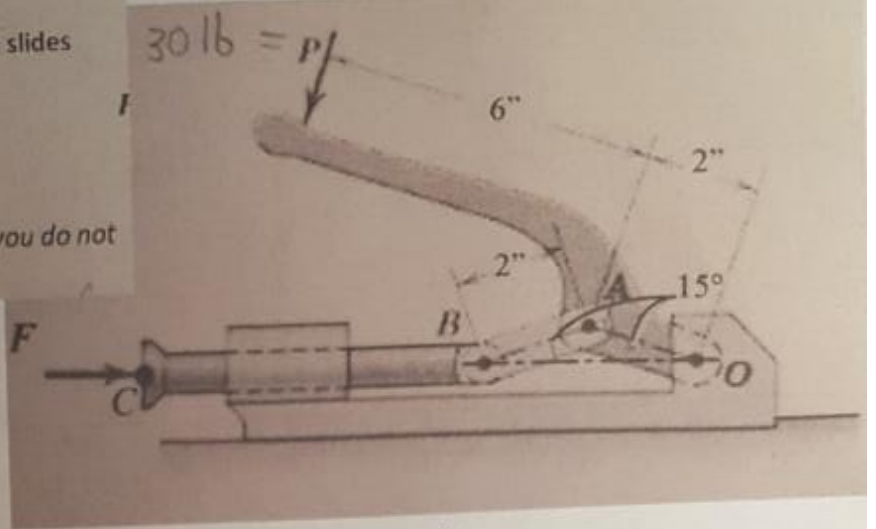
$$\begin{aligned}
 x &= \frac{M_{RA}}{F_R} \\
 &= \frac{-476 \text{ kN}\cdot\text{m}}{-70 \text{ kN}} \\
 &= 6.8 \text{ m}
 \end{aligned}$$



A force P is applied to the handle of the toggle clamp, resulting in a clamping force F at point C . The system is in equilibrium for the orientation shown. Neglect weight.

- Draw a free-body diagram of the handle.
- Draw a free-body diagram of the shaft CB , which slides freely in its smooth guide.
- Draw a free-body diagram of link AB .
- Determine the magnitudes of forces P and F .
- Determine the magnitude of the pin force at O .

You will receive no credit for parts (d) and (e) if you do not draw the free-body diagrams.



$$w/F_{AB} = 2.40$$

d) Handle: $\sum F_x = 0 = -30 \sin 15^\circ - O_x + F_{AB} \cos 15^\circ \Rightarrow O_x = 224.1 \text{ lb}$
 $\sum F_y = 0 = -30 \cos 15^\circ + O_y + F_{AB} \sin 15^\circ \Rightarrow O_y = 33.12 \text{ lb}$
 $\sum M_O = 0 = (-F_{AB} \cos 15^\circ)(2 \sin 15^\circ) - (F_{AB} \sin 15^\circ)(2 \cos 15^\circ) + 30(8)$
 $F_{AB} = \frac{240}{4 \sin 15^\circ \cos 15^\circ} = 240 \text{ lb}$

Shaft CB: $\sum F_x = 0 = F - F_{AB} \cos 15^\circ$
 $F = 240 \cos 15^\circ$
 $= \boxed{231.8 \text{ lb}}$

e) From Handle equations: $\sum F_x$ and $\sum F_y$ w/ $F_{AB} = 240 \text{ lb}$
 $O_x = 224.1$
 $O_y = 33.12$
 $O = \sqrt{O_x^2 + O_y^2}$
 $= \sqrt{224.1^2 + 33.12^2}$
 $= \boxed{226.5 \text{ lb}}$

